

$$1. f(g(x)) = f(1-x) = (1-x)^2 + 1 = x^2 - 2x + 2$$

$$g(f(x)) = g(x^2 + 1) = 1 - (x^2 + 1) = -x^2$$

$$2. a) \lim_{x \rightarrow \infty} \frac{2x+1}{3x^2+2x-7} = \lim_{x \rightarrow \infty} \frac{\frac{2x}{x^2} + \frac{1}{x^2}}{3 + \frac{2x}{x^2} - \frac{7}{x^2}} =$$

$$= \frac{0}{3} = 0$$

$$b) \lim_{x \rightarrow -2} \frac{x^2 - x - 6}{x^2 + 3x + 2} = \lim_{x \rightarrow -2} \frac{(x-3)(x+2)}{(x+1)(x+2)} =$$

$$= \lim_{x \rightarrow -2} \frac{x-3}{x+1} = \frac{-5}{-1} = 5$$

$$3. f(x) = \frac{8x}{1+x^2}$$

$$f'(x) = \frac{8(1+x^2) - 8x \cdot 2x}{(1+x^2)^2} = \frac{-8(x^2-1)}{(1+x^2)^2}$$

$$f''(x) = \frac{-16x(1+x^2)^2 + 8(x^2-1) \cdot 2(1+x^2) \cdot 2x}{(1+x^2)^4} =$$

$$= \frac{(1+x^2)(-16x - 16x^3 + 32x^3 - 32x)}{(1+x^2)^4} =$$

$$= \frac{16x^3 - 48x}{(1+x^2)^3} = \frac{16x(x^2-3)}{(1+x^2)^3} = 0$$

$$\begin{array}{ccccccc} - & & + & & - & & + \\ \hline \downarrow & -\sqrt{3} & \downarrow & 0 & \downarrow & \sqrt{3} & \downarrow \\ & & & & & & x \end{array}$$