

$$\textcircled{1} \quad 7\sqrt{2} - 3\sqrt{8} + 4\sqrt{18} = 7\sqrt{2} - 6\sqrt{2} + 12\sqrt{2} = 13\sqrt{2}$$

$$(\sqrt{90} - \sqrt{40}) \cdot \sqrt{10} = (3\sqrt{10} - 2\sqrt{10}) \cdot \sqrt{10} = \sqrt{10} \cdot \sqrt{10} = 10$$

$$(3\sqrt{5} - 2)^2 = 45 + 4 - 2 \cdot 2 \cdot 3\sqrt{5} = 49 - 12\sqrt{5}$$

$$(7\sqrt{2} - 3\sqrt{3})(7\sqrt{2} + 3\sqrt{3}) = 49 \cdot 2 - 9 \cdot 3 = 98 - 27 = 71$$

$$\textcircled{2} \quad 3\sqrt{2} > 2\sqrt{3}$$

$$6\sqrt{\frac{2}{3}} > 4\sqrt{\frac{3}{2}}$$

$$\sqrt{18} > \sqrt{12}$$

$$\sqrt{\frac{36 \cdot 2}{3}}$$

$$\sqrt{\frac{16 \cdot 3}{2}}$$

$$\sqrt{24} > \sqrt{18}$$

$$\textcircled{3} \quad \frac{\sqrt{a} + 1}{a - 1} = \frac{\sqrt{a} + 1}{(\sqrt{a} + 1)(\sqrt{a} - 1)} = \frac{1}{\sqrt{a} - 1}$$

$$\textcircled{4} \quad \frac{3}{2\sqrt{6}} = \frac{3\sqrt{6}}{2 \cdot 2} = \frac{\sqrt{6}}{4}$$

$$\frac{10}{\sqrt{14} - 2} = \frac{10(\sqrt{14} + 2)}{14 - 4} = \frac{10(\sqrt{14} + 2)}{10} = \sqrt{14} + 2$$

$$\frac{15}{\sqrt{33} + \sqrt{3}} = \frac{15(\sqrt{33} - \sqrt{3})}{33 + 3} = \frac{15(\sqrt{33} - \sqrt{3})}{36} = \frac{5(\sqrt{33} - \sqrt{3})}{12}$$

$$\textcircled{6} \quad \left(\frac{\sqrt[6]{a}}{\sqrt{a} - \sqrt{b}} + \frac{\sqrt[6]{a}}{\sqrt{a} - \sqrt{b}} \right) \cdot \frac{\sqrt{b}}{\sqrt{a} - \sqrt{b}} = \frac{\sqrt{a} \cdot \sqrt{b} + a - \sqrt{a} \cdot \sqrt{b}}{\sqrt{b}(\sqrt{a} - \sqrt{b})} \cdot \frac{\sqrt{a} - \sqrt{b}}{\sqrt{b}} = \frac{a}{b}$$